

$$\sqrt[12]{2} = 2^{\frac{1}{12}} = 1.0594 \dots$$

1779-7" 2倍

C =  $2^0 = 1$ , 261.62 Hz

C# =  $2^{\frac{1}{12}} = 1.05946$ , 277.18 Hz

D =  $2^{\frac{2}{12}} = 1.12246$ , 293.66 Hz

D# =  $2^{\frac{3}{12}} = 1.18921$

E =  $2^{\frac{4}{12}} = 1.25992$

F =  $2^{\frac{5}{12}} = 1.33484$

F# =  $2^{\frac{6}{12}} = 2^{\frac{1}{2}} = 1.4142$  減5度

A =  $2^{\frac{9}{12}} = 2^{\frac{3}{4}} = 1.68179$

B =  $2^{\frac{11}{12}} = 1.88775$

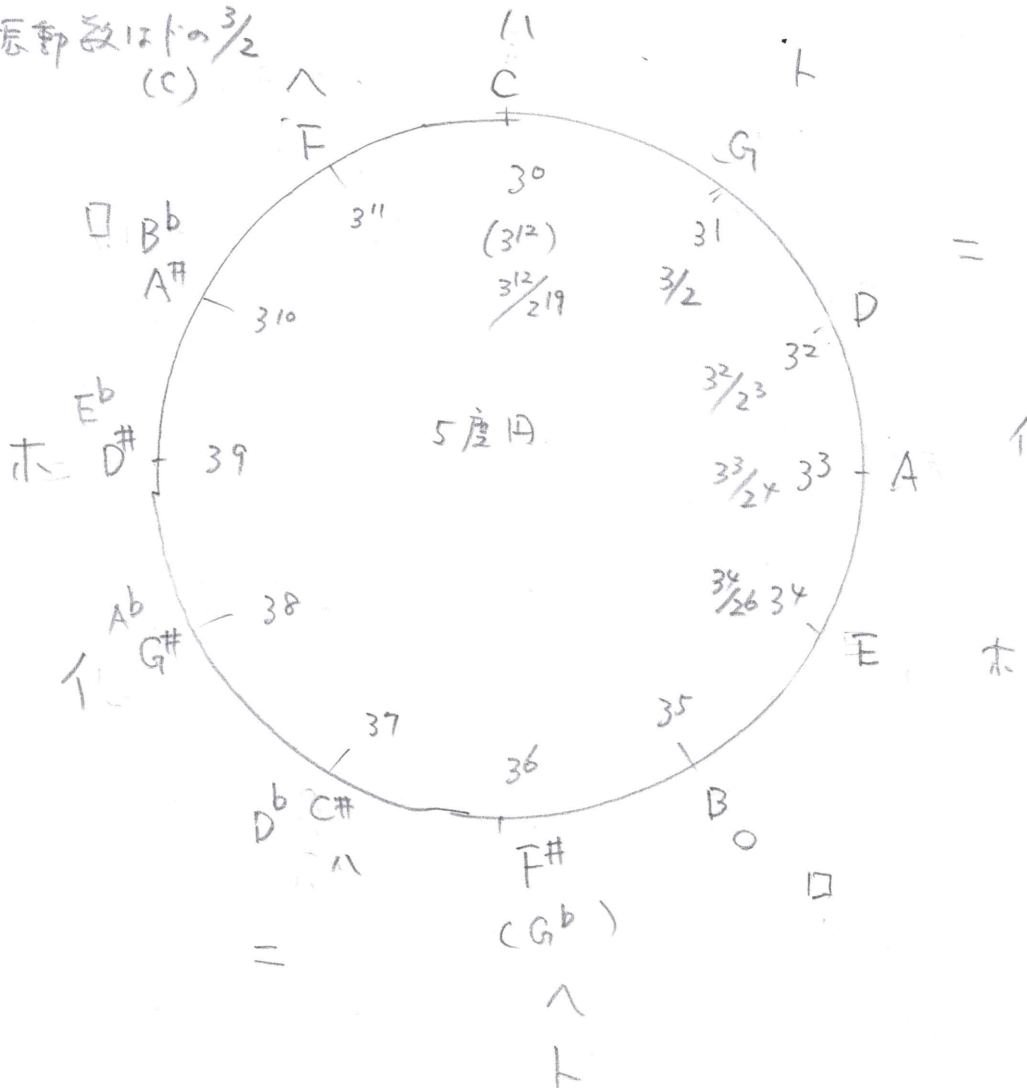
C =  $2^{\frac{12}{12}} = 2^1 = 2$

$\times 261.62 = 439.991$   
 $\approx 440 \text{ Hz}$

3倍音

1/2の振動数に12分の3/2  
 (G) (C)

$$\frac{3^{12}}{2^{19}} = 1.01364$$



ダイアトニックコード

C Dm Em F G Am Bm<sup>-5</sup>  
(Bm<sup>b5</sup>)

D<sup>b</sup> E<sup>b</sup> G<sup>b</sup> A<sup>b</sup> B<sup>b</sup> D<sup>b</sup> E<sup>b</sup>  
C<sup>#</sup> D<sup>#</sup> F<sup>#</sup> G<sup>#</sup> A<sup>#</sup> C<sup>#</sup> D<sup>#</sup>

B C D E F G A B C  
L U V U W U V U L  
ド レ ミ ファ ソ ラ シ ド

長7 (b) E7 (b) F7 G7 Am7 Bm7<sup>(-5)</sup>

C<sub>Δ</sub> Dm<sub>7</sub> Em<sub>7</sub> F<sub>Δ</sub> G<sub>7</sub> Am<sub>7</sub> Bm<sub>7</sub><sup>(-5)</sup>

diminish 減弦 半音下がる

cf. augment  
増弦 半音上がる

b → ← #  
ミ ミ ソ ソ ド ソ ソ #  
ハ イ ロ ホ イ ミ ト ♯  
ハ ロ ホ イ ニ ト ハ 長(12)

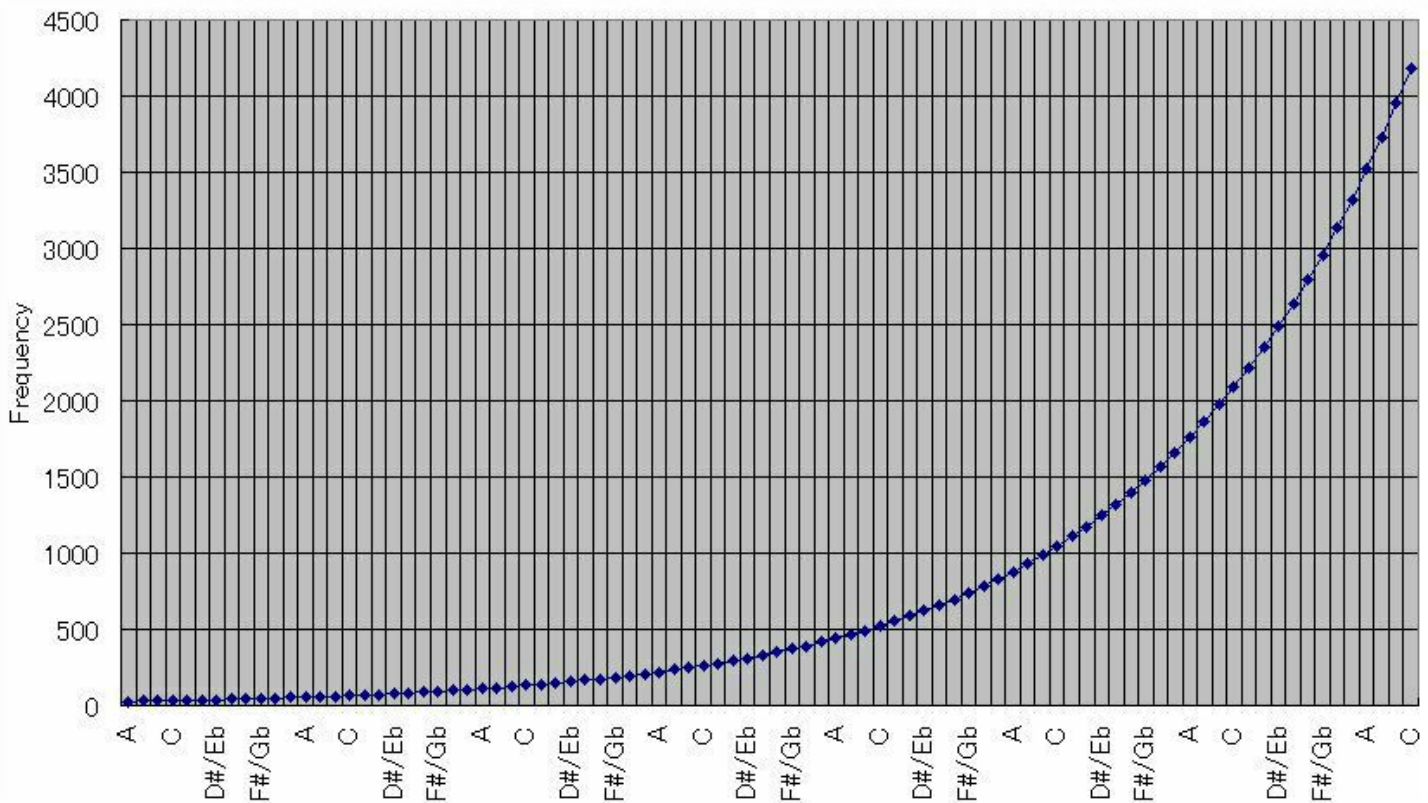
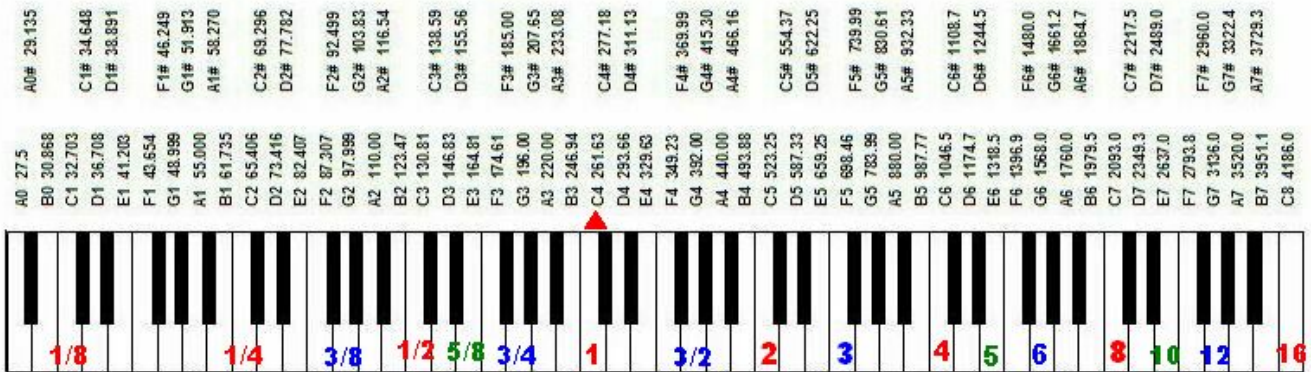
# Relationship between music theory and mathematics

## Correlation between scale and frequency

Frequency ratio  $f_n / f_o = 2^{n/12}$  (Well Temperament)

Interval	n	Ratio(Well)	Ratio(Pure)	Deviation(%)	Note	Frequency(Hz)
Unison	0	1.00000	1/1 =1.0000	0.00000	C	261.62600
Chroma	1	1.05946	135/128 =1.0547	-0.47756	C#(Db)	277.18300
2nd	2	1.12246	9/8 =1.1250	0.25380	D	293.66500
Minor 3rd	3	1.18921	6/5 =1.2000	1.07929	D#(Eb)	311.12700
Third	4	1.25992	5/4 =1.2500	-0.99210	E	329.62800
Perfect 4th	5	1.33484	4/3 =1.3333	-0.15065	F	349.22800
Diatonic tritone	6	1.41421	45/32 =1.4063	-0.79636	F#(Gb)	369.99400
Perfect 5th	7	1.49831	3/2 =1.5000	0.16929	G	391.99500
Minor 6th	8	1.58740	8/5 =1.6000	1.25989	G#(Ab)	415.30500
6th	9	1.68179	27/16 =1.6875	0.57072	A	440.00000
7th	10	1.78180	9/5 =1.8000	1.82026	A#(Bb)	466.16400
Major 7th	11	1.88775	8/15 =1.8667	-2.10820	B	493.88300
Octave	12	2.00000	2/1 =2.0000	0.00000	C	523.25100

\* The beat caused by the frequency differences between the sounds of well temperament and the pure temperament makes harmonious feeling.



# Typical chords and their frequency intervals

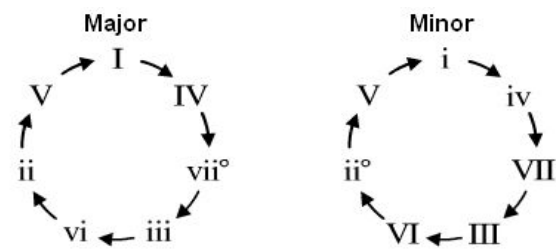
Major	Minor	7 <sup>th</sup>	Diminish	Augment	Major 7 <sup>th</sup>	9 <sup>th</sup> , 11 <sup>th</sup> , etc.
-------	-------	-----------------	----------	---------	-----------------------	---

3 <sup>rd</sup> (0.99%)	Min 3 <sup>rd</sup> (1.08%)	3 <sup>rd</sup> (0.99%)	Min 3 <sup>rd</sup> (1.08%)	3 <sup>rd</sup> (0.99%)	3 <sup>rd</sup> (0.99%)
5 <sup>th</sup> (0.17%)	5 <sup>th</sup> (0.17%)	5 <sup>th</sup> (0.17%)	Dia 3(-0.8%)	Min 6 <sup>th</sup> (1.26%)	5 <sup>th</sup> (0.17%)
		7 <sup>th</sup> (1.82%)	6 <sup>th</sup> (0.57%)		Maj 7 <sup>th</sup> (-2.11%)

<-- Children's song, Enka, Folk, Rock -->  
 <----- Classical music ----->  
 <----- Popular music, Latin ----->  
 <----- Jazz, Fusion ----->

# Chord Progression

I      IV      vii<sup>o</sup>      iii      vi      ii      V      I  
 C      F      G7      Em      Am      Dm      G      C



# Rhythm recognition for automatic transcription

MIDI Signal

→

score

*estimation*

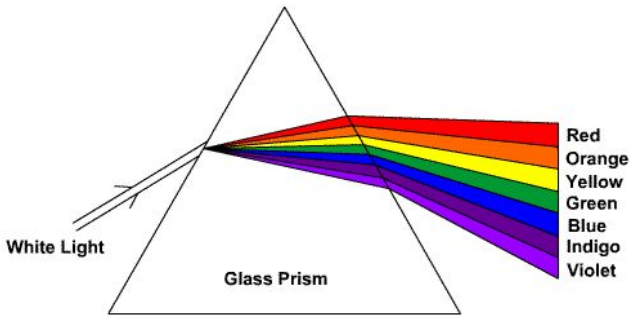
(IOIs) [sec]
(note value) [beat]

# Music marks for expression

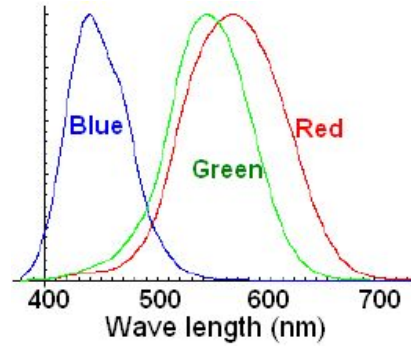


# Construction of tone color (Wave form)

Light spectrum makes color

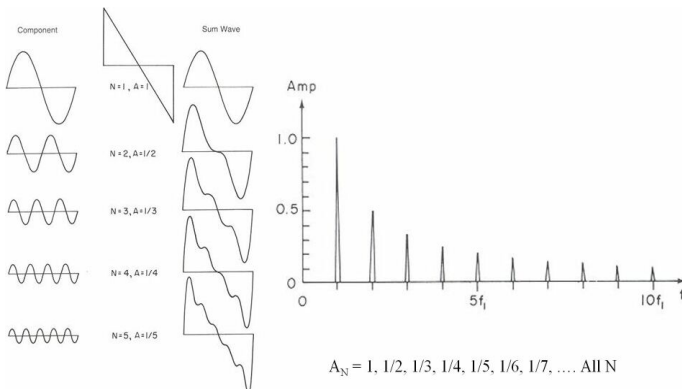


Relative spectral sensitivity of the three types of cones in the human retina

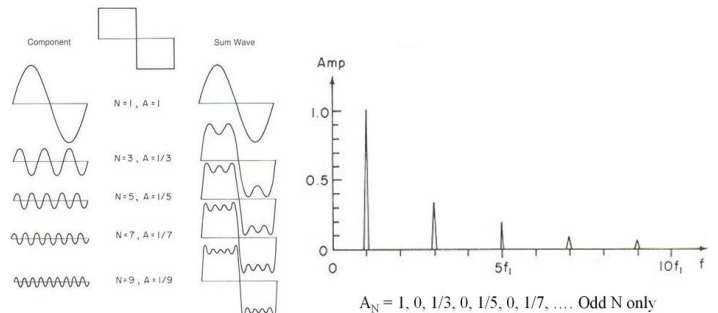


Sound spectrum makes tone color

\* Tooth Wave



\* Square Wave (Sounds like clarinet)



# ADSR envelope

The contour of the ADSR envelope is specified using four parameters:

**Attack** : How quickly the sound reaches full volume after the sound is activated (the key is pressed).

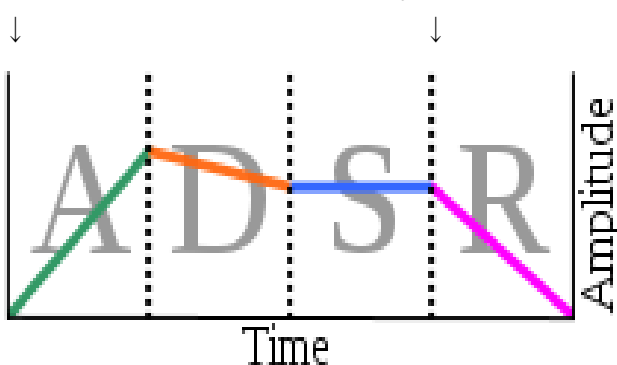
**Decay** : How quickly the sound drops to the sustain level after the initial peak.

**Sustain** : The "constant" volume that the sound takes after decay until the note is released.

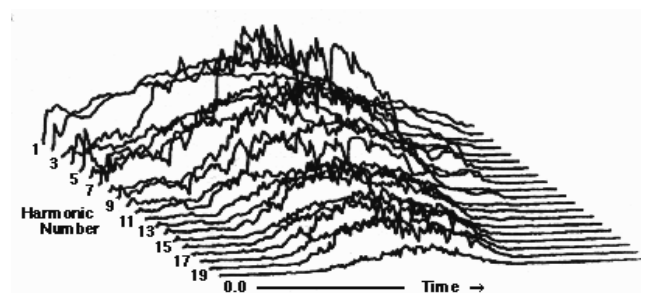
**Release** : How quickly the sound fades when a note ends (the key is released). Often, this time is very short.

Key-pressed

Key-released



# Spectrum envelope



<http://www.sfu.ca/sonic-studio>

# 音程・コードの確認ですよ！

全音 長2度  
半音 短2度

学園坂

1. 次の2音の音程と転回した音程も書いてください。

Handwritten labels: 短6, 長3, 短6, 長3, 長7, 短2, 長5, 短4, 長4, 短5, 短4, 増4, 減5

解答例：完全4°&完全5°

Handwritten labels: 減5, 増4, 長7, 短2, 長5, 短4, 短2, 長7, 短7, 短2, 減5, 増4, 長2, 長7, 短6, 長3

Handwritten labels: 増4, 減5, 短4, 長5, 短7, 長2, 短3, 長6, 長3, 短6, 減5, 長6, 短6, 長3

Handwritten labels: 短2, 長7, 長6, 短3, 短6, 長3

2. 次の和音のコードネームを書いてください。

Handwritten chord names: E<sub>m</sub>, F, G<sub>m</sub>, D<sub>m</sub>/F, C<sub>#m</sub>-5, F<sub>#m</sub>-5, E, B<sub>m</sub>-5, B<sub>b</sub>, B, C<sub>#m</sub>, C<sub>#</sub>∅

Handwritten chord names: F<sub>#</sub>, G<sub>7</sub>, C<sub>#m</sub>7, F<sub>7</sub>, B<sub>m</sub>7, G<sub>#7</sub>dim, E<sub>b</sub>7, A<sub>7</sub>, G<sub>7</sub>, E<sub>m</sub>7

Handwritten chord names: Bdim, D<sub>m</sub>7, E<sub>7</sub>, E<sub>7</sub>/F<sub>#</sub>, C<sub>7</sub>, C<sub>m</sub>7, C<sub>m</sub>-5, C<sub>m</sub>7, D<sub>m</sub>∅7, E<sub>∅7</sub>, C<sub>∅7</sub>, C<sub>m</sub>∅7

Handwritten chord names: C<sub>m</sub>∅7